

## ANALYSIS OF VARIATION OF THE BIAS POINT WITH VOLTERRA SERIES METHOD IN CLASS-AB RF POWER AMPLIFIER

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**Abstract**—This paper presents a Volterra-series bias based circuit of Class-AB RF power amplifier. This circuit design is power and accurate for nonlinear circuits. In Class-AB RF PA design, and analyze with bias circuit and it makes balance between efficiency and linearity, which make the application of the Volterra-series bias circuit is more flexible in practical applications. The measurement result verifies the effectiveness of this design and a test die is fabricated.

**Keywords**—Volterra Series bias circuit; Class AB power amplifier (PA); efficiency; nonlinearity.

### I. INTRODUCTION

A power amplifier is basically an electronic circuit which transfers the RF power to the load by amplifying the input power. To meet the simultaneous requirements of high linearity and reasonable efficiency, RF power amplifiers are often operated in a class-AB mode which is a compromise between Class-A and Class-B in terms of efficiency and linearity. Class-A PA always operates at high collector current, result in high linearity and high power dissipation. Class-B PA is more efficient than Class-A PA, but the low bias point brings worse linearity. Class-AB PA operates at relative low bias point, however the bias point rise with the increased input power due to the self-biasing effect, the reason is in Class-AB operation the conduction angle is a function of drive level. In BJT or HBT PA, this effect is shown as rising average biasing current along with increasing input power.

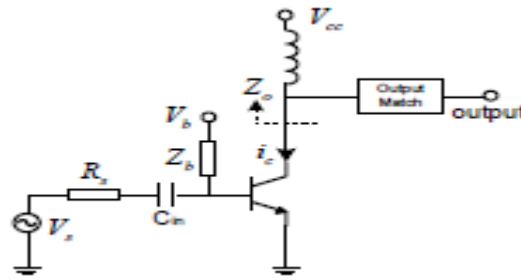
The working current is low at low input power can improve the efficiency and the bias point can rise at high input power to enhance the linearity of the PA. In order to improve the realization of Class-AB PA, it is essential to find out how the input power function with changes of bias point.

The reason of self-biasing effect with suffers both conduction and cut-off and the charge and discharge time constants are asymmetry in a signal period, the B-E junction of BJT or HBT. The bias point is nonlinear with input power. For small signal analysis, to determine the nonlinear distortions of PAs and BJT/HBT device in particular, the well-known Volterra series design technique is widely used [1-5]. Also, there are some papers that have discussed gaining an optimum linearity with optimized bias points or harmonic impedance terminations [6-8].

In this work, to analyze the variation of the bias point quantitatively, the Volterra series analysis method has been used in common emitter (CE) power amplifier. Consequently the period of PA's design and experiment can be shortened. According to the theoretical analysis, the optimum bias circuit parameters which promise the bias point varies with the input power sensitively is obtained, so the PA can reach higher performance. A test die is fabricated and the measurement result verifies the effectiveness of this design technique.

### II. THE PRINCIPLE OF SELF BIASING EFFECT

The static bias point and dynamic bias point are two kinds of bias points in amplifier. Static bias point is the bias voltage and current independent of input signal and which is totally determined by external static bias circuit. Dynamic bias point contains the static component and along with the components caused by average value of asymmetrical voltage or current at large input signal. So the dynamic bias point of PA is concern with the conduction angle. The larger bias point, the greater The higher bias point, the greater DC component of  $i_c$ . Saturation output power of PA is relative to the DC component of  $i_c$ , the higher of this component the greater of the output power.



In Fig1. CE power amplifier.

$i_c$  is the collector current of CE amplifier transistor. In this amplifier, bias circuit impedance  $Z_b$  has great effect on the charge and discharge circuit of BE junction.  $Z_b$  is too small may cause much signal power dissipated in bias circuit and power input  $P_{in}$  is lower into the amplifier, so the self biasing is weakened and the amplifier's gain is reduced. When  $Z_b$  decreased to 0, where  $P_{in}=0$  amplifier, the bias point is independent of  $P_{in}$  relative constant, so the variation of  $i_c$  is also small and the self biasing is insignificant too. When  $Z_b=$  too large and increased to the greatest limit, the bias circuit is equivalent to constant current bias circuit, and the bias point always keeps the same. As above analysis, both too large and too small  $Z_b$  would prevent bias point increase with high input power. In order to obtain the optimum self biasing effect,  $Z_b$  value should be optimized in PA's design.

### III. DERIVATION OF THE BIAS POINT WITH VOLTERRA SERIES

The movement of the bias point of PA is a nonlinear process, so we should use nonlinear analyze technique to do this studies.

#### A. Volterra Series Method

Volterra series is an effective mathematical design technique to analyze the nonlinear time-invariant system with memory [6].

Assume the input  $V_s$  to the nonlinear circuit is:

$$V_s(t) = \sum_{r=1}^R E_r e^{j\omega_r t} \quad \text{-----(1)}$$

Then, the response  $V_o$  is:

$$V_o(t) = \sum_{k=1}^{\infty} V_{o,k}(t) \quad \text{-----(2)}$$

In which,  $V_{o,k}$  is the  $k$ -th order response of the circuit

$$V_{o,k}(t) = (\sum_{r1=1}^R E_{R1} \dots \sum_{rK=1}^R E_{RK} \dots)$$

$$G_K(\omega_{R1} \dots \omega_{RK}) e^{j(\omega_{R1} + \dots + \omega_{RK})t} \quad \text{---(3)}$$

$G_K(\omega_{R1} \dots \omega_{RK})$  is  $k$ -th order transfer function.

#### B. Nonlinear Model For Common Emitter Amplifier:

The nonlinear equivalent model for CE power amplifier is shown in Fig. 2. In the equivalent circuit, base-emitter resistance  $r_{be}$ , base-emitter capacitance  $C_{be}$  and trans conductance,  $g_m$  are the major contributors to nonlinearity.

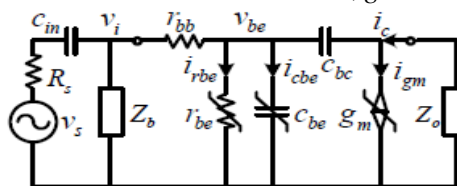


Fig2: Nonlinear equivalent model for CE power amplifier.

The current through  $r_{be}$  can be expressed as: [9]

$$i_{r_{be}} = g_1 v_{be} + g_2 v_{be}^2 + g_3 v_{be}^3 \quad \text{-----(4)}$$

The current generated by  $g_m$  is  $\beta$  times of the current through  $r_{be}$  in which  $\beta$  denotes current gain [10].

$$i_{gm} = \beta g_1 V_{be} + \beta g_2 V_{be}^2 + \beta g_3 V_{be}^3 \text{ -----(5)}$$

The charge of  $C_{be}$  can be expressed as:

$$q_{cbe} = C_{be1} V_{be} + C_{be2} V_{be}^2 + C_{be3} V_{be}^3 \text{ -----(6)}$$

### C. Volterra Series Derivation

Write the following equations for each node of Fig. 2 using Kirchoff's current laws (KCL):

$$\left. \begin{aligned} \frac{V_{be} - V_i}{r_{bb}} &= \frac{V_i - V_s}{R_s + 1/j\omega C_{in}} \\ \frac{V_{be} - V_i}{r_{bb}} &= i_{rbe} + i_{cbe} + j\omega C_{be}(V_{be} + i_c Z_o) \\ j\omega C_{bc}(V_{be} + i_c Z_o) + i_c &= i_{gm} \end{aligned} \right\} \text{-----(7)}$$

Based on the equations (7)

above,  $V_{be}$  can be expressed as:

$$V_{be,1}(\omega) = \frac{1}{A_1(\omega)} Z_b(\omega) / \{ [Z_b(\omega) + r_{bb}] (R_s + 1/j\omega C_{in}) + Z_b(\omega)r_{bb} \} \text{ -----(8)}$$

$$V_{be,2}(\omega_1, \omega_2) = \frac{A_2(\omega_1 + \omega_2)}{A_1(\omega_1 + \omega_2)} V_{be,1}(\omega_1) V_{be,1}(\omega_2) \text{ -(9)}$$

$$\left. \begin{aligned} A_1(\omega) &= (g_1 + j\omega C_{bc}) + \frac{j\omega C_{bc}[Z_o(\omega)\beta g_1 + 1]}{j\omega C_{bc}Z_o(\omega) + 1} \\ &+ \frac{1}{r_{bb} + \frac{Z_b(\omega)(R_s + \frac{1}{j\omega C_{in}})}{Z_b(\omega) + R_s + \frac{1}{j\omega C_{in}}}} \\ A_2(\omega) &= (g_2 + j\omega C_{bc2}) + \frac{j\omega C_{bc}Z_o(\omega)\beta g_2}{j\omega C_{bc}Z_o(\omega) + 1} \\ I_{c,1}(\omega) &= \frac{\beta g_1 - j\omega C_{bc}}{j\omega C_{bc}Z_o(\omega) + 1} V_{be,1}(\omega) \end{aligned} \right\} \text{--(10a & 10b)}$$

$$\left. \begin{aligned} I_{c,2}(\omega_1, \omega_2) &= \frac{[\beta g_1 - j(\omega_1 + \omega_2)C_{bc}]V_{be,2}(\omega_1 / \omega_2)}{j(\omega_1 + \omega_2)C_{bc}Z_o(\omega_1 + \omega_2) + 1} \\ &+ \frac{\beta g_2 V_{be,2}(\omega_1)V_{be,2}(\omega_2)}{j(\omega_1 + \omega_2)C_{bc}Z_o(\omega_1 + \omega_2) + 1} \end{aligned} \right\} \text{--(11a & 11b)}$$

While the input is  $\sin V_s = A \sin \omega t$  which is the DC component of  $i_c$  can be expressed as:

$$i_{c0} = \frac{1}{2} A^2 I_{c,2}(\omega, -\omega) = \frac{A^2}{2} \frac{\beta g_1}{g_1 r_{bb} + g_1 Z_b(0) + 1} |V_{be,1}(\omega)|^2 \text{ -(12)}$$

From the equation (14),  $Z_b$  has significant influence on  $i_c$ . Due to  $i_c$  is in proportion to the source power, it can be normalized using source power:

$$i_{c0}/P_{in} = 4R_s I_{c,2}(\omega, -\omega) \text{ -----(13)}$$

$i_{c0}/P_{in}$  has no concern with the strength of input power, so it could be evaluated the variation range of the bias point with the input power.

### D. Calculated Results And Analysis

Considering the output matching network is lossless, the power gain of PA is:

$$A_P = 4 |I_{c,1}(\omega)|^2 R_s \text{Re}(Z_o) \text{ -----(14)}$$

The power gain is also closely connected with  $Z_b$ . The major parameters of a real 700MHz CE power amplifier are shown in Table I.

Table I: MAJOR PARAMETERS OF A REAL CE POWER AMPLIFIER

$r_{bb}$ $\Omega$	$g_1$ A/V	$g_2$ A/V <sup>2</sup>	$g_3$ A/V <sup>3</sup>	B
0.07	87	0.065	1.0	8.3
$C_{bc}$	$C_{be1}$	$C_{be2}$	$C_{be3}$	
5.3	42	0.32	4.3	

According to the formulas (13) and (14), the variation range of bias point and power gain of the amplifier are shown in Fig. 3. From Fig. 3, we can conclude the best value of  $Z_b$  is  $6\Omega$ , when  $Z_b < 5\Omega$ , power gain is low and when  $Z_b > 7\Omega$ , the variation range of bias point is small.

#### IV. MEASUREMENTS AND CONCLUSION

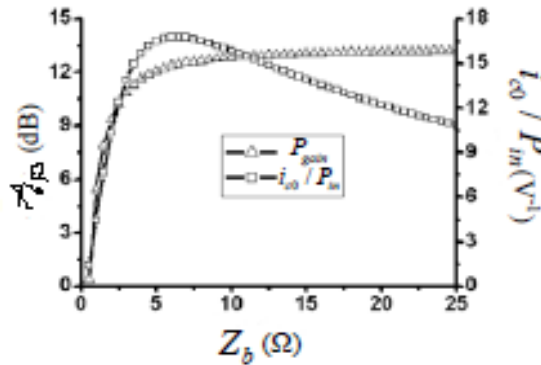


Fig. 3. Variation range of bias point and power gain of CE power amplifier.

Biassing the amplifier in Class AB mode through adjusting the external  $Z_b$  and  $v_b$  to make the static bias current density is equivalent to  $2\text{kA/cm}^2$ . Table II shows the measurement results in different  $Z_b$ , in which  $i_{c0}/P_{in}$  is measured with 4dBm input power. As can be seen in table II, has the same variation law with the output power of 1dB compression point, so the AM-AM feature of the amplifier could be improved through optimizing  $i_{c0}/P_{in}$  value, and this improvement in linearity is achieved in the case of maintaining a constant quiescent bias current,

TABLE II. MEASUREMENT RESULTS OF CE AMPLIFIER

$Z_b$ ( $\Omega$ )	$A_p$ (dB)	$I_{c0}/P_{in}$ ( $V^{-1}$ )	$P_{-1}$ (dBm)
3.9	11.2	16	20.2
4.7	11.5	16.3	23.0
5.1	11.9	17	24.1
7.5	12.4	17.1	24.3
15	12.9	14.6	21.6
20	13.0	13.8	19.3

and therefore without increasing static power amplifier to ensure the efficiency of the amplifier.



Fig. 4. Die photo of the fabricated CE power amplifier and test bench.

Here, Fig. 4 is the die photo of CE power amplifier. The amplifier is fabricated with  $2\mu\text{m InGaP/GaAs HBT}$  process. The measurement result is compare with the theoretical analysis, so this design can be used in class AB PA to simplify the PA's design and experiment.

#### ACKNOWLEDGMENT

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