

ANALYSIS AND DESIGN OF TAPERED PILES WITH CORRUGATIONS IN SANDY SOIL CONDITION

Er Devesh Ojha¹, Er Ramsha Khan²

¹*Assistant Professor, Civil Engineering Department Amity University, Lucnow (UP), India.*

²*Assistant Professor, Faculty of Civil Engineering SRMU, Lucnow (UP), India.*

Abstract- *Our main motive under this topic is to investigate behaviour of tapered piles under various soil conditions and examine their feasibility. We have added another feature into the tapered piles, and that is of corrugated surfaces. The corrugation can be either semi-circular or square in shape. The advantages of using corrugated surface is that the cylindrical surface area of piles is increased which further leads to an increase in skin friction, thus the load carrying capacity of the piles.*

Keywords- *Corrugations, group pile, skin friction. tapered pile, square tapered piles*

I INTRODUCTION

Our main motive with this research work is to investigate the behaviour of tapered piles under various soil conditions and examine their feasibility. "Corrugated surfaces" have been added to the tapered piles which can be either semi-circular or square in shape. This addition leads to an increase in the cylindrical surface area of piles further causing an increase in skin friction, thereby enhancing the load carrying capacity of the piles.

Based on the shape tapered piles can be classified as:-

- Circularly tapered piles
- Square tapered piles
- Based on the shape of corrugations, the tapered piles are divided as:-
 - Tapered piles with circular corrugations
 - Tapered piles with square corrugations
- Based on technique of construction we have -
 - Normal tapered piles
 - Step tapered piles

Our aim is to analyze tapered piles and calculate their area and circumference followed by computation of load bearing capacities both as individual and group piles. A detailed design including the amount of reinforcement, pile cap group piles followed by cost assessment and feasibility analysis is done. Thus, we have decided to introduce a system of corrugations on the surface of tapered piles along its length to let its cylindrical surface area increase that would lead to enhancement in load carrying capacity of piles. Two basic types of corrugations will be introduced "semi-circular and square followed by computation of the base and cylindrical areas of the foundation. Some advantage of using tapered piles :-

- Tapered piles are easy to drive into the soil due to their changing cross sections, low at bottom and high at top.
- Tapered piles offer high amount of frictional resistance for same base area due to increased cylindrical surface area.
- Tapered piles enhance the load carrying capacity and strength of piles.
- Tapered piles compact soils in the vicinity to enhance its strength.
- Tapered piles are efficient in operation.
- The number of tapered piles as a group is reduced for the same area and same amount of load to be resisted as compared to normal vertical piles.
- Tapered piles are cost effective.

II METHODOLOGY

Tapered piles corrugated length: -

These corrugation enhance the surface area have the skin friction also increases leading to an increased capacity of tapered piles we consider these corrugations a semicircular in shape.

- Let us assume that 10 corrugations are present in 1 cm so the length of 1 cm changes to

$$= [9.090 \times 10^{-4} \times 6 + 5 \times \frac{\pi L}{2} \times 9.090 \times 10^{-4}]m$$

i.e. Semi-circular and b plain areas in 10 corrugations

$$1 \text{ cm} = 0.012595 \text{ m}$$

$$\text{Thus in } 1m = 100 \text{ cm} = 1.2595 \text{ m}$$

Thus for a surface with corrugations

$$l = 1.2595 \text{ m}$$

Thus corrugated surface increase the cylindrical surface area of piles, thus its skin friction resistance.

Tapered Piles - Corrugated Semicircular

<i>Circular Vertical Piles</i>	<i>Square vertical piles</i>	<i>Circularly tapered piles</i>	<i>Square tapered piles</i>	<i>Step tapered piles</i>
Diameter d= 0.3m	Width = 0.3 m, thickness = 0.3 m	Top diameter = 0.6 m (d ₁) Bottom diameter = 0.3 m (d ₂)	Top width = 0.6 m (a) Top thickness = 0.6 m (t1) Bottom width = 0.3 m (b) Bottom thickness = 0.3 m (t2)	Divided into 6 parts of 2 m each Bottom dia (d ₂) = 0.20 m Top dia (d ₁) = 0.35 m
Length = 12 m	Length = 12 m	Length = 12 m. (l)	Length (l) = 12 m	Length = 18 m
At each part the diameter in areas by 2.5 cm				

Assumed data in the analysis

Analysis of tapered sections

- Circularly tapered sections

Let, d₁ = top diameter, d₂ = bottom diameter, L = length of pile

Consider any section of length dx let dia be D_x at this point

$$\text{So, } D_x = D_1 - \left(\frac{D_1 - D_2}{L}\right) x$$

$$D_x = D_1 - Kx$$

$$\text{Where } K = \left(\frac{D_1 - D_2}{L}\right)$$

- To calculate the volume we need to integrate the area of each such strips throughout the length

Total volume

$$v = \int_0^l \frac{\pi}{4} dDx^2 = \frac{\pi}{4} \int_0^l (D_1 - Kx)^2 dx$$

$$v = \frac{\pi}{4} \left[D_1^2 x + K^2 \frac{x^3}{3} - 2D_1 K \frac{x^2}{2} \right]_0^l$$

$$v = \frac{\pi}{4} \left[D_1^2 l + K^2 \frac{l^3}{3} - 2D_1 K \frac{l^2}{2} \right]$$

$$\text{Now, } A = \frac{v}{L}$$

For Example: As per Our assumptions

$$d_1 = 0.6 \text{ m, } \quad d_2 = 0.3 \text{ m, } \quad l = 12 \text{ m}$$

$$K = \frac{d_1 - d_2}{l} = \frac{0.6 - 0.3}{12} = 0.025$$

Now,

$$v = \frac{\pi}{4} \left[(0.6)^2 \times 12 + \frac{0.025^2 \times 12^3}{3} - \frac{2 \times 0.6 \times 0.025 \times 12^2}{2} \right]$$

$$v = \frac{\pi}{4} [4.32 + 0.36 - 2.16]$$

$$v = 1.979 \text{ m}^3$$

$$A = \frac{1.979}{12} = 0.165 \text{ m}^3$$

Now we read to calculate cylindrical surface area of the square tapered piles

Perimeter of section X-x = πD_x

$$= \pi [D_1 - Kx]$$

For the length l of pile

$$\text{Slanting length} = l_s = \sqrt{P^2 + B^2}$$

$$= \sqrt{12^2 + 0.15^2} = 12.00093 \text{ m}$$

$$\text{Cylindrical as} = \int_0^l \pi D_x = \int_0^l \pi (D_1 - Kx) dx$$

$$\text{Surface area} = A_s = \pi \left[D_1 x + K \frac{x^2}{2} \right]_0^l$$

$$\text{Top perimeters} = \pi d_1; A_s = \pi \left[D_1 l + K \frac{l^2}{2} \right]$$

$$\text{Bottom perimeters} = \pi d_2; A_s = \pi (d_1 + d_2) \times l_s^2$$

$$\text{Average} = \frac{\pi}{2} (d_1 + d_2)$$

$$d_1=0.6\text{m}, d_2=0.3\text{m}, l_s= 12.00093 \text{ m}$$

For corrugated surfaces,

$$l \text{ m}=1.2595 \text{ m} ; 12.00093 \text{ m}= 15.1152 \text{ m}$$

$$\text{Now, } A_s = \frac{\pi}{2} (d_1 + d_2) \times l_s = \frac{\pi}{2} (0.6 + 0.4) \times 15.1152 = 23.74 \text{ m}^2$$

Let a= top width; b= bottom width; t₁= top thickness; t₂= Bottom thickness

At section x-x the width

$$W_x = (a - k_1 x)$$

$$\text{Where; } K_1 = \frac{a-b}{L}; \text{ thickness } t_x = (t_1 - k_2 x); K_2 = \frac{t_1 - t_2}{2}$$

Now we used to calculate is volume by integrating area of each strip of width W_x and thickness b_x, throughout the length

$$A_x = W_x \times t_x = (a - k_1 x) (t_1 - k_2 x) = at_1 - ak_2 x - k_1 t_1 x + k_1 k_2 x^2$$

Now volume ,

$$v = \int_0^l [at_1 - ak_2 x - k_1 t_1 x + k_1 k_2 x^2]$$

$$v = [at_1 x - ak_2 \frac{x^2}{2} - k_1 t_1 \frac{x^2}{2} + k_1 k_2 \frac{x^3}{3}]$$

$$v = at_1 l - ak_2 \frac{l^2}{2} - k_1 t_1 \frac{l^2}{2} + k_1 k_2 \frac{l^3}{3}$$

$$\text{now } A = \frac{v}{L}$$

assuming the data a=0.6 m, b=0.3m, t₁=0.6m, t₂=0.3m, l=12m

$$\text{so, } k_1 = \frac{a-b}{L} = \frac{0.6-0.3}{12} = 0.025; k_2 = \frac{t_1-t_2}{L} = \frac{0.6-0.3}{12} = 0.025$$

$$v = 0.6 \times 0.6 \times 12 - 0.6 \times 0.025 \times \frac{12^2}{2} - 0.025 \times 0.6 \times \frac{12^2}{2} + 0.025 \times 0.025 \times \frac{12^3}{3}$$

$$v = (4.32 - 1.08 - 1.08 + 0.36)m^3; v = 2.52 \text{ m}^2$$

$$\text{Now } A = \frac{v}{L} = 0.21 \text{ m}^2$$

Now we read to calculate cylindrical surface area of the square tapered piles

$$\text{Top perimeter} = 2(a + t_1); \text{ Bottom perimeter} = 2(b + t_2)$$

$$\begin{aligned} \text{Average of the two} &= \frac{1}{2} \times 2(a + b + t_1 + t_2) \\ &= (a + b + t_1 + t_2) \end{aligned}$$

Now cylindrical surface area = $(a + b + t_1 + t_2) \times L_s$

where; L_s = slanting length of tapered pile;

$$L_s = \text{slanting length of tapered pile} = \sqrt{P^2 + B^2} = \sqrt{12^2 + 0.15^2} = 12.00093 \text{ m}$$

Now assuming corrugated surface

$$L_s = 12.00093 \text{ m} = 15.1152 \text{ m}; a = 0.6 \text{ m}, b = 0.4 \text{ m}, t_1 = 0.6 \text{ m}, t_2 = 0.4 \text{ m}$$

So $A_s = (a + b + t_1 + t_2) \times L_s$

$$= (0.6 + 0.4 + 0.6 + 0.4) \times 15.1152 = 30.2304 \text{ m}^2$$

Thus we have effectively calculated the area, and cylindrical surface area of two main types of tapered piles.

1. Circularly tapered piles
2. Square tapered piles

Now we need to compute load bearing capacities or each.

INDIVIDUAL TAPERED PILES

LOAD BEARING CAPACITY

For any pile type or soil conditions the basis formula to calculate bearing capacity is

$$Q_f = q_f A_b + F_s A_s$$

Where,

Q_f = ultimate load bearing capacity of pile

A_b = area of pile at base

q_f = ultimate load capacity of strata on which piles is supported

F_s = average ultimate friction of shearing resistance of soil per unit area

A_s = cylindrical surface area of pile (perimeter x length)

I. In sand

Method 1 : we have $Q_f = q_f A_b + f_s A_s$

Where ; $q_f = \gamma D_f N_q$;

D_f = depth of pile embedded in sand ;

γ = Effective overburden pressure at bottom or base of pile

N_q = values of N_q for drivers pile vary as - :

Φ in degree	Value of N_q	
	$\frac{Df}{B} = 25$	$\frac{Df}{B} = 50$
28	12	9
30	7	14
32	25	22
34	40	37
36	58	56
38	89	88
40	137	136

$$F_s = k_s \bar{q}_0 \tan \delta$$

\bar{q}_0 = Average effective over burden pressure acting along Embedded length; $\bar{q}_0 = \frac{rDf}{2}$

δ = friction angle b/w pile surface and surrounding sand

value of δ = 0.75 for concrete pill

= 20 for steel pile

K_s = average coefficient of lateral Earth pressure acting along any embedded length D_f

= 1.0 for loose sands

= 2.0 for dense sands

Method 2 :

Computing ultimate Bearing of pile by SPT-N value method

$$O_f = q_f A_b + F_s A_s$$

Now, $q_f = 40 N \frac{Df}{B}$ [Limited to 400 N]

where, N is SPT-N value in visibility of pile base

$F_s = 2 N$ where \bar{N} is SPT N value averaged rear embedded depth of pile

(i) Circulatory tapered piles

Problem: - We need to calculate the ultimate load bearing capacity of circularly tapered piles with varying diameter in sands and compare the same with ultimate load bearing capacity of normal vertical circular piles.

Assumptions: - As per the practical observations we assume the following data

Tap dia of tapered pile = $d_1 = 0.6$ m

Bottom dia of tapered pile = $d_2 = 0.3$ m

Dia of normal vertical pile	0.3 m
Length of pile	12 m
Corrugated length of pile	5.1152 m
Friction angle of sand	40°
K - value of dense	2.0
Dry unit weight of sand	8 KN/M^3

Solution : (a) For vertical circular pile ultimate load carrying capacity

$$Q_f = q_f A_b + F_s A_s$$

where; $q_f = r D f N_q$; $N_q = \text{B.C. failure}$; $N_q = \tan^2(45 + \frac{\phi}{2}) e^\pi \tan \phi$

$$\text{So; } N_q = \tan^2\left(45 + \frac{40}{2}\right) e^\pi \tan 40^\circ = 64.194$$

$$\text{Hence, } q_f = r D f N_q = 18 \times 12 \times 64.194 = 13865.904 \text{ KN/m}^2$$

$$\text{Also, } F_s = K_s \bar{q}_0 \tan \delta$$

where $K_s = K = 2$

$$\delta = 0.75 \phi \text{ (ascrete pile)} = 30^\circ, 20^\circ \text{ (still corrugators)}$$

$$\bar{q}_0 = \frac{r D f}{2}$$

$$\text{So; } F_s = 2 \times \frac{1}{2} \times 18 \times 12 \times \tan 20^\circ = 78.62 \text{ KN/m}^2$$

$$\text{Now, } A_b = \text{area of base} = \frac{\pi}{4} (0.3)^2 = 0.07068 \text{ m}^2; A_s = \pi d \times D_f = \pi \times 0.3 \times 12 = 11.3097 \text{ m}^2$$

$$Q_f = q_f A_b + F_s A_s$$

$$Q_f = 13865.904 \times 0.07068 + 78.62 \times 11.30 = 1869.128 \text{ KN}$$

$$\text{Now using } F_{os} = 2.5, \text{ So safe load } Q = \frac{Q_f}{F_{OS}} = \frac{1869.128}{2.5} = 747.652 \text{ KN}$$

(b) For circularly tapered piles

$$\text{Value of } q_f = 13865.904 \text{ KN/m}^2; \text{ Value of } F_s = 78.62 \text{ KN/m}^2$$

Now, for circularly appeared piles, as use now already calculated.

$$A_b = \frac{\pi}{4} (0.3)^2 = 0.07068 \text{ m}^2 \text{ and } A_s \text{ (for corrugated surface)} = 23.74 \text{ m}^2$$

$$\text{now } Q_f = q_f A_b + F_s A_s, Q_f = 13865.904 \times 0.07068 + 78.62 \times 23.74 = 2846.480 \text{ KN}$$

Now using $F_{os} = 2.5$

So safe load $Q = \frac{Q_f}{FOS} = \frac{2846.480}{2.5} = 1138.592 \text{ KN}$

(c) Comprising of normal vertical circular pile and circularly tapered pile.

$$= \frac{\text{Safe load for tapered pile}}{\text{Safe load for vertical pile}} = \frac{1138.592 \text{ KN}}{747.652 \text{ KN}} = 1.523$$

Result: Thus circular tapered piles can bear loads about 1.523 times higher than normal vertical piles, thus are more effective in use.

(ii) Square tapered piles

Problem: - We need to calculate the ultimate load bearing capacity of square tapered pile with varying width and thickness in sands and compare the same with ultimate load bearing capacity of normal vertical square piles.

Assumptions: As per the practical observations we assume the following data:-

1	Top width of square pile (a)	0.6 m
2	Bottom width of square pile (b)	0.3 m
3	Top thickness of square pile (t ₁)	0.6 m
4	Bottom thickness of square pile (t ₂)	0.3 m
5	Length of piles	12 m
6	Corrugated length of piles	15.115 m
7	Friction angle of dense sand	40°
8	Dry unit weight of sand	18KN/m ³
9	K - value of dense sand	2.0

Solution :

(a) For vertical square pile ultimate load carrying capacity

$$Q_F = q_F A_b + f_s A_s$$

For sands with same value of friction angle and piles of same length (12m), the

$$\text{value of } q_F = 13865.904 \text{ KN/m}^2; f_s = 78.62 \text{ KN/m}^2$$

$$A_b = (0.3 \times 0.3) = 0.09 \text{ m}^2; \quad A_s = 4 \times 0.3 \times 12 = 14.4 \text{ m}^2$$

So, $Q_F = q_F A_b + f_s A_s = 13865.904 \times 0.09 + 14.4 \times 78.62 = 2380.06 \text{ KN}$

Using FOS = 2.5 ; So safe load $Q = \frac{Q_f}{FOS} = \frac{2380.06}{2.5} \text{ KN}$

$$Q = 952.024 \text{ KN}$$

(b) **For tapered square pile**

Ultimate load carrying capacity

$$Q_F = qFA_bFsAs$$

Value of $F_s = 78.62 \text{ KN/m}^2$

Now, for tapered square piles, as we have calculated

$$A_b = (0.3)^2 = 0.09 \text{ m}^2 \text{ and } A_s \text{ (corrugated length)} = 30.2304 \text{ m}^2$$

$$\text{Now } Q_F = 13865.904 \times 0.09 + 30.2304 \times 78.62 = 3624.645 \text{ KN}$$

$$\text{using FOS} = 2.5, \text{ Safe load } Q = \frac{Q_F}{\text{FOS}} = \frac{3624.645}{2.5} = 1449.86 \text{ KN}$$

(c) **Comparision of normal vertical square pile and tapered square pile**

$$\frac{\text{Safe load for tapered pile}}{\text{Safe load for vertical pile}} = \frac{1449.86 \text{ KN}}{952.024 \text{ KN}} = 1.523$$

Result : Thus square tapered piles with varying width and thickness can bear to ads about 1.523 times higher than normal vertical care, hence are more effective in use.

III CONCLUSION

With all the noted advantages of using tapered piles our observations include a major finding that the cylindrical surface area is prominent factor in enhancing the load carrying capacity of tapered piles. The tapered piles hold immense potential to bring a revolution in the construction industry and should be tested for other medias also.

IV REFERENCES

- Cased cast in situ concrete piles, Soil mechanics and foundations by B.C. Punmia and A.K. Jain.
- Load carrying capacity of pile foundations, Soil mechanics and foundation engineering by S.K. Garg.
- Analysis of uniformly tapered circular and rectangular bars, Strength of materials by Dr. R.K. Bansal.
- Design of slender columns and pile caps, Reinforced concrete limit state design by A.K. Jain.
- Raymond step-tapered concrete piles, Soil mechanics and foundations by B.C. Punmia and A.K. Jain.