

TOLERANCE SYNTHESIS OF 3R PARALLEL ROBOT MANIPULATOR

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Abstract— This paper focus on the tolerance synthesis of a parallel robot manipulator with 3R revolute joints. The present work deals with making the dimensions of the robot manipulator robust and compute the optimal dimensional tolerances for a given 3R parallel robot manipulator for minimising the positioning error of end effector of robot with given target. For making the dimensions robust a proper robustness index has to be chosen. Obtained robust dimensions must tolerate globally to largest variations. Then to compute the optimal dimensional tolerances from the given robust dimensions a new tolerance synthesis method developed by Stephane Caro is used. This method is known as Caro-Tolerance box method. The optimal dimensional tolerances are calculated by optimal dimensional algorithm. The values of robustness index and optimal dimensional tolerances are validated.

Keywords— robust design, tolerances, optimal, variations, sensitivity, robustness index, tolerance synthesis, 3R parallel manipulator

1. INTRODUCTION

Parallel manipulators possess significant advantages over serial manipulator in terms of dynamic properties, load-carrying capacity, high accuracy as well as stiffness. This is because parallel manipulators are characterized by several kinematic chains connecting the base to the end-effectors, which allows the actuators to be located on or near the base of the manipulator. Therefore, parallel manipulator can be used in many applications where these properties are of primary importance while a limited workspace is acceptable.

Gough built the first hexapod to test tires. This parallel manipulator is commonly referred to as “Gough-Stewart platform” and now generally accepted in the robotics and manipulators community. But the most common application of parallel manipulators is in flight simulation, as originally proposed by Stewart. Although flight simulators have been used for several years, Hunt introduced the concept of parallel manipulator and suggested, using this type of manipulator in robotics. Since then, parallel manipulators have been given considerable attention. The number of applications in which parallel manipulators are used has been steadily increasing and several prototype manipulators have been built. For instance, parallel manipulators can also be used as machine tools or even for medical purpose. So far, many types of parallel manipulators have been proposed. Other applications of parallel manipulators are adjustable articulated trusses, walking machines and high-speed, high-precision, multi d.o.f machining centre.

There are some factors limiting the application of parallel manipulators. One main factor is that the workspace of parallel manipulators is quite limited, because the closed-loop nature of parallel manipulators limits the motion of the platform. The other one is that singular configuration, the number of degrees of freedom of the manipulator changes instantaneously. If the manipulator gains one or more degrees of freedom, it becomes uncontrollable. Furthermore, in such a singular configuration, the actuator forces can become very large, which may result in a breakdown of the manipulator.

Most of the 6-dof parallel manipulators studied to date consist of six extensible limbs. These parallel manipulators possess the advantages of high stiffness, low inertia, and large payload capacity

2. Robust Design problem for 3R Robot Manipulator

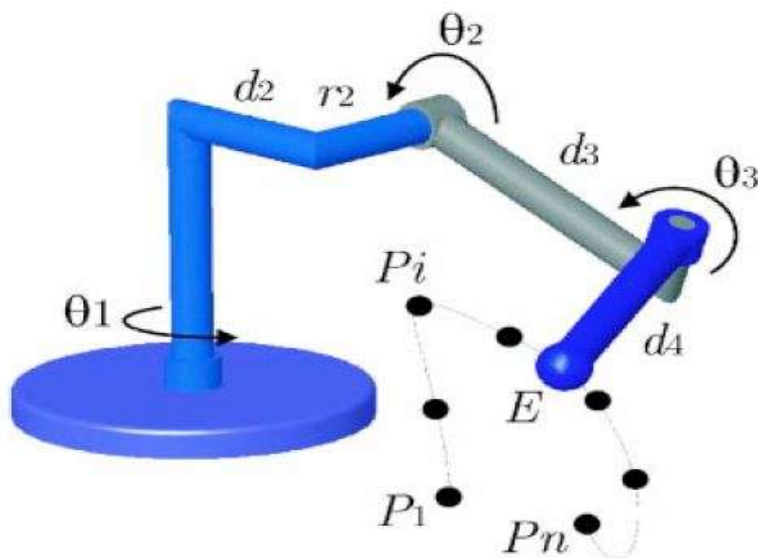


FIG 13 R robot manipulator

according to [7] In every robust design problem, the difference is made between three sets: (i) the set of design variables (*DV*); (ii) the set of design parameters (*DP*); (iii) the set of performance functions. in the present work of 2R serial robot manipulator mechanism design variables are link lengths and design variables are force acting on the manipulator and coefficient of friction between the link lengths. The l -dimensional vector of design variables is denoted by $\mathbf{x} = [x_1, x_2, \dots, x_l]^T$. The m -dimensional vector of design parameters is denoted by $\mathbf{p} = [p_1, p_2, \dots, p_m]^T$. Performance functions are grouped into the n -dimensional vector $\mathbf{f} = [f_1, f_2, \dots, f_n]^T$. *Design Variables* are subjected to uncontrollable variations because of manufacturing errors, wear, or other uncertainties, .According to [] A mechanism is robust when the sensitivity S of its performances to variations is a minimum. Therefore, S can be defined as the ratio of the Euclidean norm of variations in its performances, $\|\delta f\|_2$, and the Euclidean norm of variations in *DV* and *DP*, $\|\delta X\|_2$.

$$\mathbf{f} = \mathbf{f}(\mathbf{x}, \mathbf{p}) \quad (2.1)$$

$$\delta \mathbf{f} = [\mathbf{J}_x \mathbf{J}_p] [\delta \mathbf{x}^T \delta \mathbf{p}^T]^T = \mathbf{J} d\mathbf{X} \quad (2.2)$$

According to [7] S represents a variation transmission ratio and means the amount of variations transmitted from the sources to the design. Besides, eq.(2.3) follows from eq.(2.2) and means that S is bounded by the smallest singular value, σ_{\min} , and the largest singular value, σ_{\max} , of sensitivity Jacobian matrix \mathbf{J} .

$$\sigma_{\min} \leq S = \frac{\|\delta f\|_2}{\|\delta X\|_2} \leq \sigma_{\max} \quad (2.3)$$

3. Robustness Indices

In order to obtain a robust solution independently of the amount of variations in *DV* and *DP*, a judicious robustness index is required. The robustness indices usually found in the recent literature are the condition number and the Euclidean norm of the sensitivity Jacobian matrix, \mathbf{J} . Al-Widyan and Angeles [7], Ting and Long [8] used the condition number of \mathbf{J} . Zhu [9] and Hu et al. [10] suggested the use of the Euclidean norm of \mathbf{J} . In this section, it is shown that the Euclidean norm of \mathbf{J} is more appropriate for the robust design of mechanisms. The condition number of a matrix is the ratio of its largest singular value to its smallest singular value. Let RI_1 be the condition number of \mathbf{J} .

$$RI_1 = \|J\|_2 \|J^{-1}\|_2 = \frac{\sigma_{\min}}{\sigma_{\max}} \quad (3.1)$$

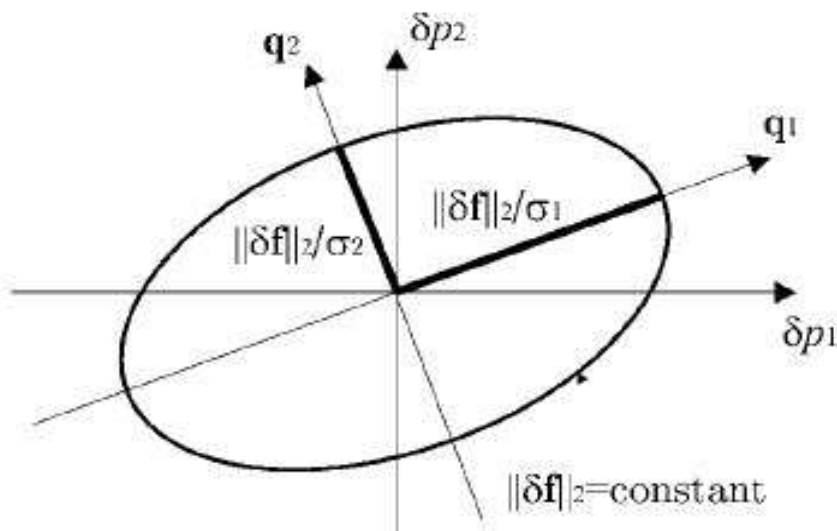


Fig 2. Design sensitivity ellipsoid

As there are several robust manipulators, the designer can choose another criterion to be optimized. For instance, he can take into account the cost or the complexity of the mechanism. Here, the optimal robust manipulator is supposed to be the one with the best dexterity. This criterion is frequently used in manipulator design. It evaluates the ease of a manipulator to execute motions or arbitrary motions in all directions. It is quantified by the condition number of its kinematic Jacobian matrix. The smaller the condition number, the higher the dexterity. Besides, the manipulator is isotropic when its condition number is equal to one. Let J_k be the kinematic Jacobian matrix of the 2R manipulator:

$$J_k = \begin{pmatrix} C_1 & -S_1 & C_2 C_1 \\ S_1 & C_1 & C_2 S_1 \\ 0 & 0 & S_2 \end{pmatrix} \quad (3.2)$$

$$S_1 = \sin \theta_1$$

$$S_2 = \sin \theta_2$$

$$C_1 = \cos \theta_1$$

$$C_2 = \cos \theta_2$$

5. CARO-TB tolerance synthesis method

[1] Some works in the literature deal with the link between dimensional tolerances and product cost. Here, the cost of a mechanism is supposed to decrease when its dimensional tolerances increase. Thus, a new tolerance synthesis method is proposed, which aims at finding the largest tolerance box of a mechanism that does not include rejects. Let $j(C)$ be the design sensitivity ellipsoid of a mechanism corresponding to a norm of variations in its performance equal to C . Assuming that this norm has to be smaller than C , the optimal tolerance box is supposed to be the largest box included in $j(C)$. This tolerance box called Caro-TB [1] is smaller than Zhu-TB, but does not include any reject. The choice of the tolerance box depends on the wish of the designer. However, it is always important to know the solution without rejects because the cost of the loss due to rejects can be estimated from this solution. First, nominal values $x = [x_1 x_2 \dots x_n]^T$ of design variables are computed from robustness index RI_2 presented in Section 3. Then, their optimal dimensional tolerances $\Delta x_{i,opt}$ are computed using the following optimization algorithm.

6. Design Optimization Algorithm

$$\begin{aligned} & \{ \max |b_1 b_2 b_3| \\ & \text{s.t. } U(b_1, b_2, \dots, b_i) \in \xi_{mr} \end{aligned}$$

$$\begin{aligned} b_1 &\geq 0 \\ b_3 &\geq 0 \\ |b_i| &\geq \Delta x_{i \min}, \quad i=1, \dots, 3. \end{aligned}$$

$$\text{where } \Delta x_{1 \min} = 1 \mu\text{m}, \quad \Delta x_{2 \min} = \frac{r_2}{d_2} \Delta x_{1 \min}, \quad \Delta x_{3 \min} = \frac{d_3}{d_2} \Delta x_{1 \min}$$

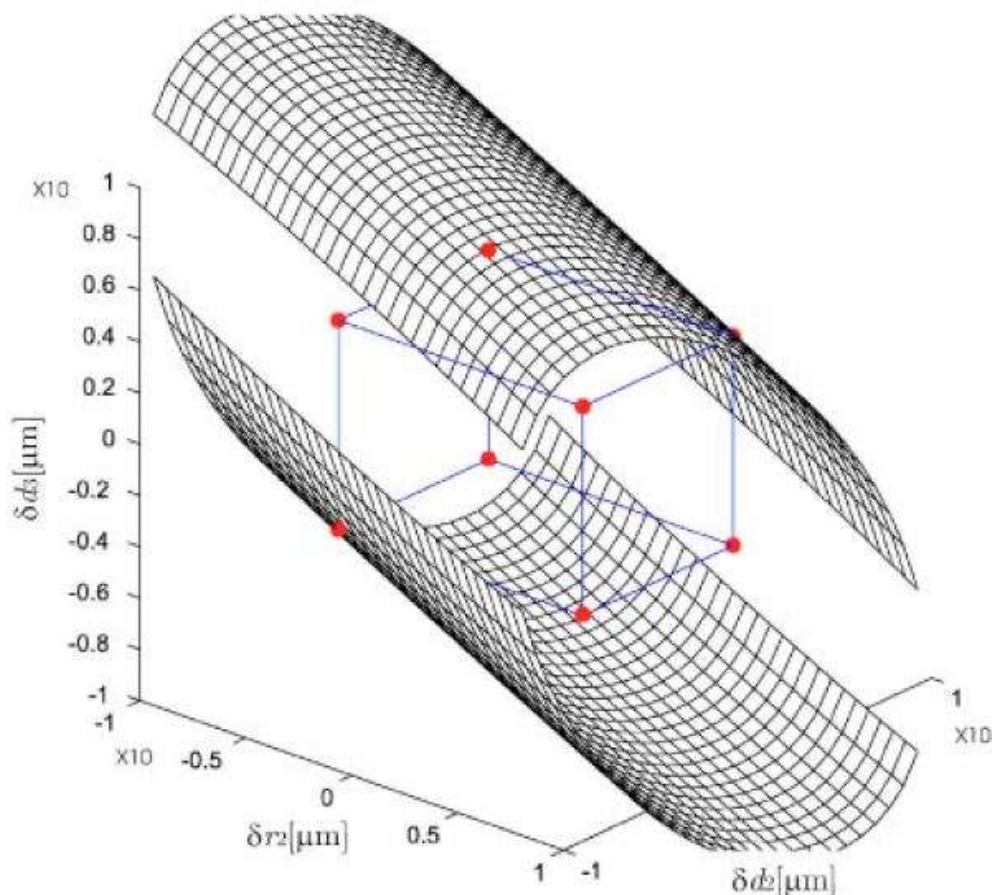


Fig. 2 The most restrictive ellipsoid and the optimal tolerance box

7. Results and Discussions

The results of this optimization problem are:

$$b_1 = 4.07 \mu\text{m} \quad b_2 = -5.67 \mu\text{m} \quad b_3 = 4.07 \mu\text{m}$$

Figure 16 depicts the values of E when $\delta d_2, \delta r_2, \delta d_3$ are between $-\Delta d_{2opt}$ and Δd_{2opt} , $-\Delta r_{2opt}$ and Δr_{2opt} , $-\Delta d_{3opt}$ and Δd_{3opt} respectively, and for the five poses of the manipulator. E is always smaller than 10 mm. It means that the positioning error of E is smaller than 10 mm for any posture of the manipulator when the tolerances of d_2, r_2 , and d_3 are $\Delta d_2, \Delta d_3, \Delta r_2$, respectively. Points $B_1(1,0,0), B_2(-1,0,0), B_3(0,-1,0), B_4(0,1,0), B_5(0,0,1)$, and $B_6(0,0,-1)$ belong to all design sensitivity ellipsoids of the manipulator because a unitary variation of a design variable and no variation of the others lead to a unitary variation of the position of E . As an ellipsoid is a convex volume, octahedron $B_1, B_2, B_3, B_4, B_5, B_6$ depicted in Fig. 17 is included in all the design sensitivity ellipsoids of the manipulator such that a point on the surface leads to a positioning error of E equal to 10 mm. It follows that Eq. 16 is a sufficient condition for the positioning error of E to be smaller than 10 mm whatever its pose:

$$\Delta d_2 + \Delta r_2 + \Delta d_3 \leq 10 \mu\text{m} \tag{7.1}$$

Without the tolerance synthesis method proposed, the designer would have chosen dimensional tolerances by means of $\Delta d_2, \Delta d_3, \Delta r_2$ does not respect Here, $\Delta d_{2opt}, \Delta d_{3opt}, \Delta r_{2opt}$, do not

Respect 7.1 because $\Delta d_2 + \Delta r_2 + \Delta d_3 = 13.81\text{mm}$. It means that the optimal tolerance box is not included in octahedron $B_1, B_2, B_3, B_4, B_5, B_6$, as depicted by Fig. 17. However, they allow the positioning error of E to be smaller than 10 mm at each pose $P_i, i=1,2,\dots,5$. So, knowing the target of the manipulator, the tolerance synthesis method proposed is more interesting than the sufficient condition, defined by Eq. 16!, to synthesize its dimensional tolerances.

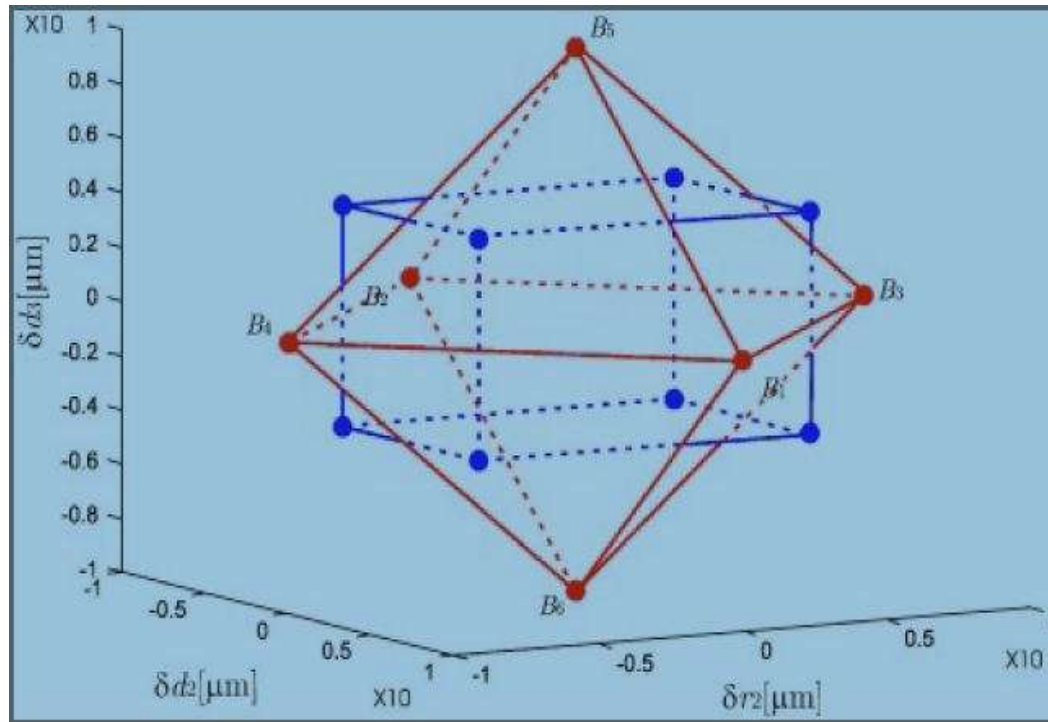


Fig 3. Caro optimal Tolerance Box[1]

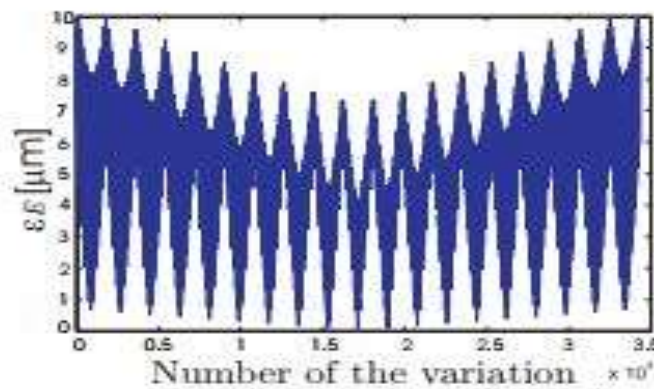


Fig4 Validation of optimal tolerance box

8. Conclusions.

This paper has given an effective tolerance synthesis technique for components, in view of a powerful plan approach. The investigation of the vigor of a system takes after two back to back advances, which are free and reciprocal. The initial step goes for processing its strong measurements by methods for a suitable heartiness record. The Euclidean norm of the sensitivity Jacobian framework is such a list. The investigation of a damper affirmed that the Euclidean norm of its sensitivity Jacobian lattice is more appropriate than its condition number, to measure the heartiness of an instrument. This technique yields the arrangement of all the hearty manipulators and enables the architect to incorporate other criteria. At that point, the created tolerance synthesis strategy is utilized to register the ideal tolerance box of the chose hearty controller. The hypothesis is shown by two serial manipulators. The utilization of this hypothesis to the hearty plan and tolerance synthesis of parallel manipulators is one of the following stages in our examination work.

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